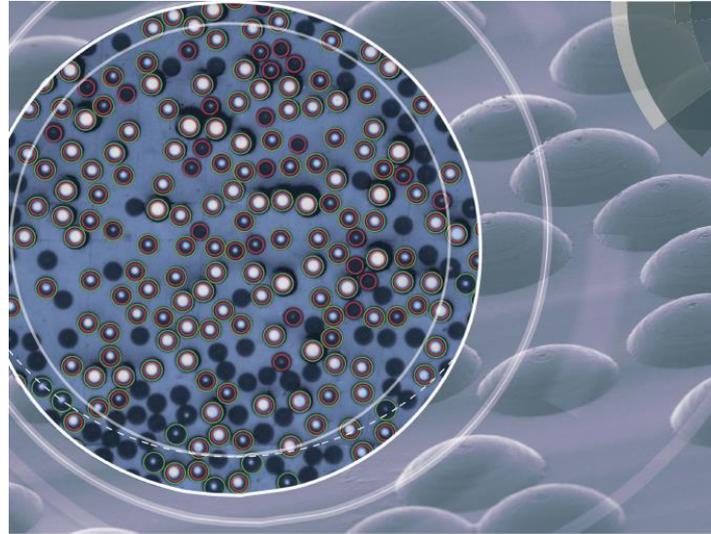


Normal contact and friction of rubber with model randomly rough surfaces



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V. Romero, A. Prevost & E. Wandersman

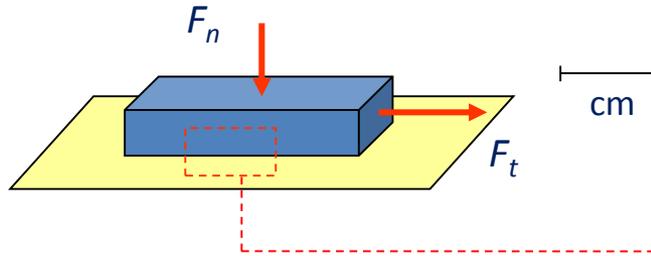
Jean Perrin Laboratory (LJP), Université P. et M. Curie, Paris, France



M.K. Chaudhury

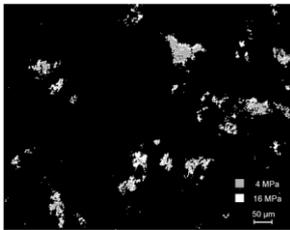
Department of Chemical Engineering, Lehigh University, Bethlehem, USA

Friction between macroscopic bodies: a longstanding problem....



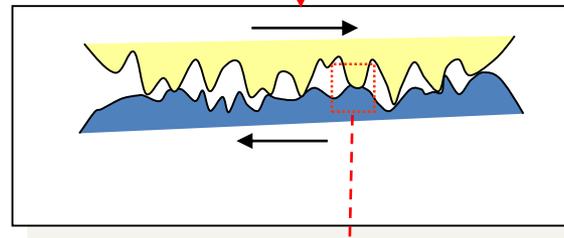
• Surface geometry & contact mechanics

Actual contact area \ll Apparent contact area



JH Dietrich & BD Kilgore, Technophys 1996

Surface roughness → multi-contact interface

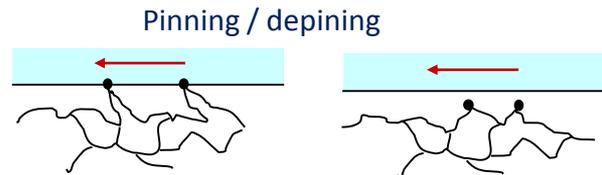


$\mu\text{m} - \text{cm}$

Bowden & Tabor, 1950's

• Surface physical-chemistry

Molecular scale dissipative processes



Rubbers

Schallamach, 1963

Rough contacts mechanics

- Non adhesive single asperity elastic contacts

Hertz (1881)

- Adhesive contact between smooth surfaces

JKR & DMT (1971)

- Contact between nominally flat surfaces

Greenwood & Williamson (1966)

Real contact area $A \propto P$

→ Justification of Amontons-Coulomb's friction law

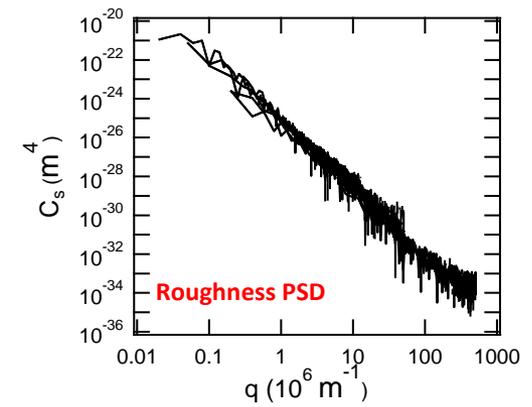
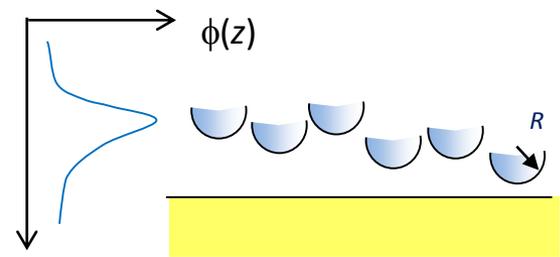
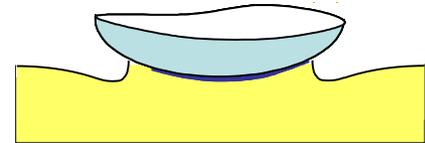
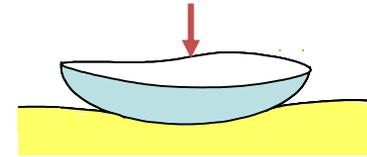
→ Extensions to more complex geometries

Archard (1957), Ciavarella (2008)...

- Rough contact models based on a spectral description of surface topography

Persson (2001), Robbins (2007), Müser (2008)...

→ Extensions to friction and adhesive contacts



Scope

Transparent randomly rough surfaces consisting in distributions of spherical asperities ($\sim 50 \mu\text{m}$)

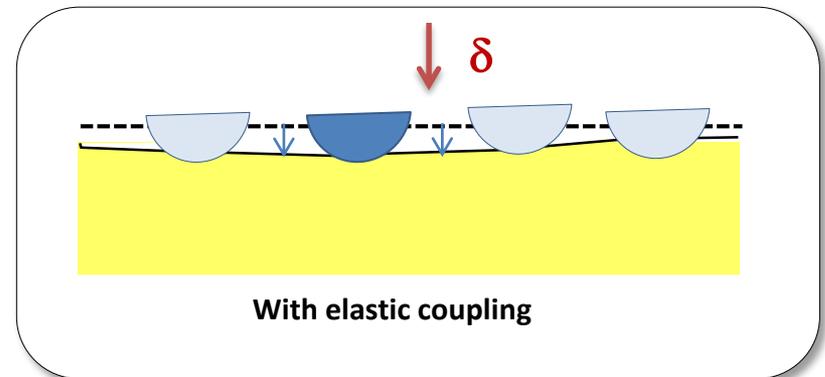
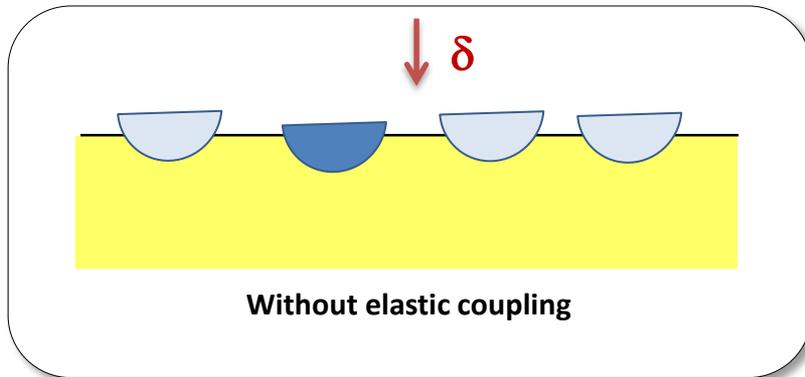
GW type surfaces

Imaging of micro-contacts distributions



Load dependence of the real contact area $A(P)$
+
Statistical distributions of micro-contacts pressure and size

Role of elastic coupling between asperities ?

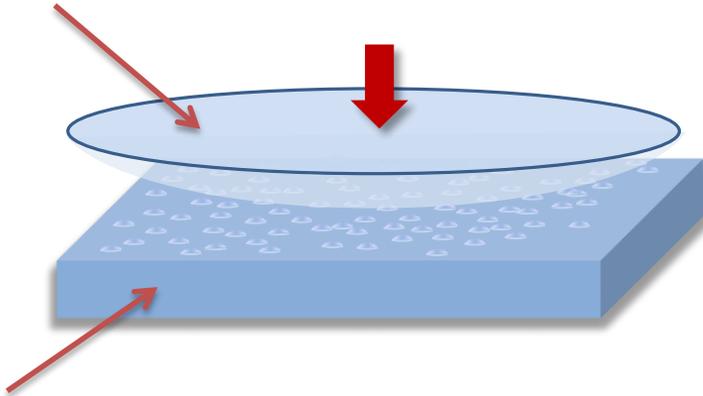


GW model

Patterned surfaces and associated sphere-on-plane contacts / I

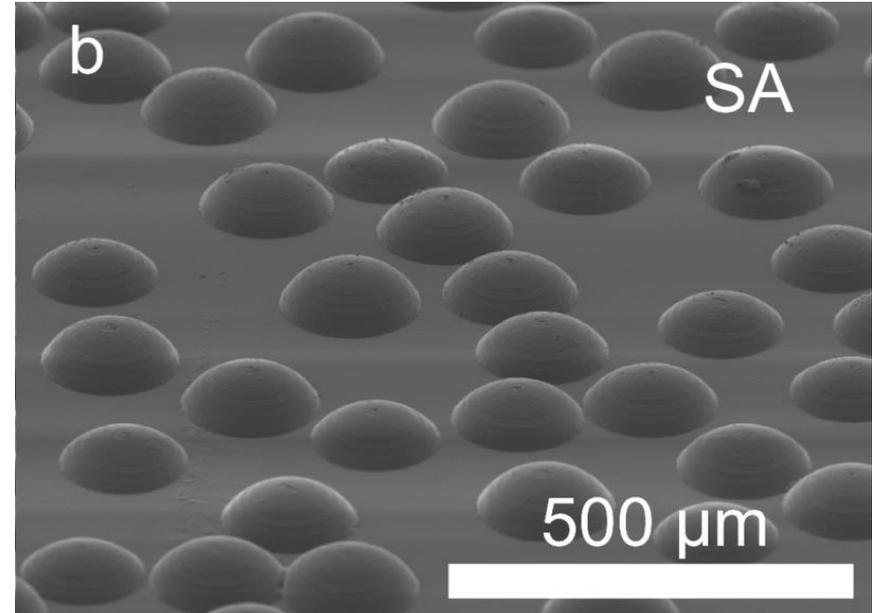
- Soft Asperities (SA) surfaces

Smooth glass lens ($R=128$ mm)



Patterned elastic PDMS substrate

Surface density: $\phi = 0.1$ and 0.4



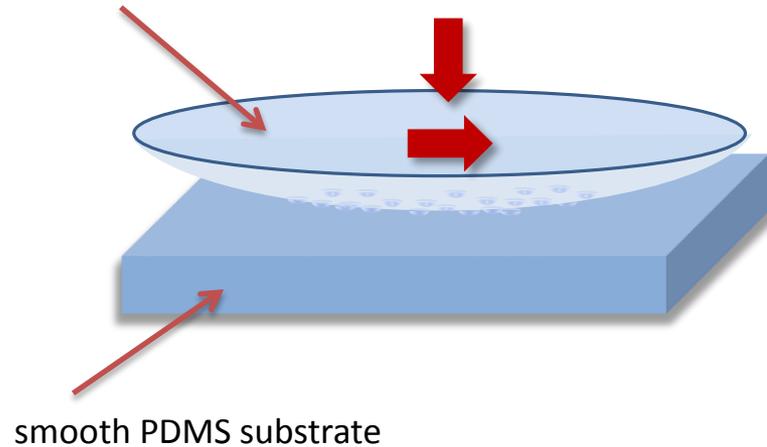
Replication of a micro-machined PMMA template

- Lateral and height distributions of spherical asperities perfectly controlled by design
 - Uniform random height distribution ($R=100$ μm , 30 $\mu\text{m} < \text{height} < 60$ μm)
- Small scale roughness on the micro-asperities → normal contact experiments only

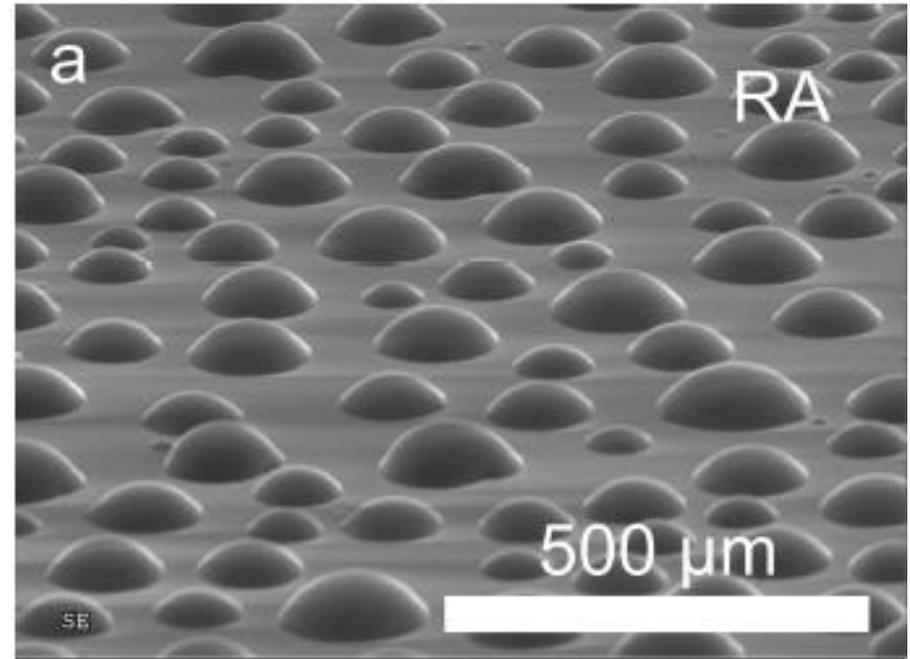
Patterned surfaces and associated sphere-on-plane contacts /II

- Rigid Asperities (RA) surfaces

Patterned glass lens ($R=13$ mm)



Surface density: $\phi=0.41$

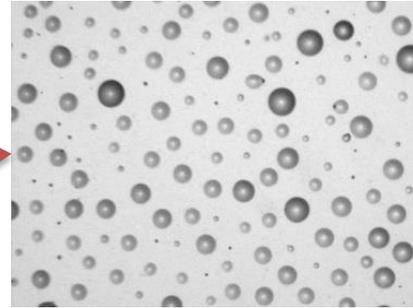
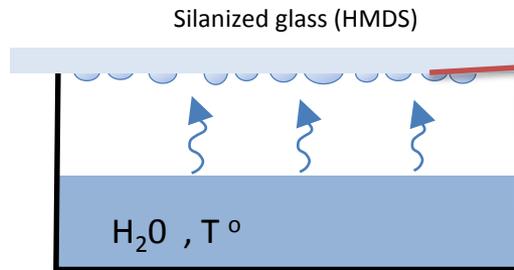


- Gaussian distribution of asperity sizes and heights (a posteriori characterization)
- Smooth micro-asperities \rightarrow normal contact and friction experiments

Water droplet condensation method....

Fabrication of rigid asperities patterns by droplet condensation method

• 1. Water droplet condensation



Time of exposure to water vapor

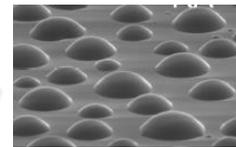
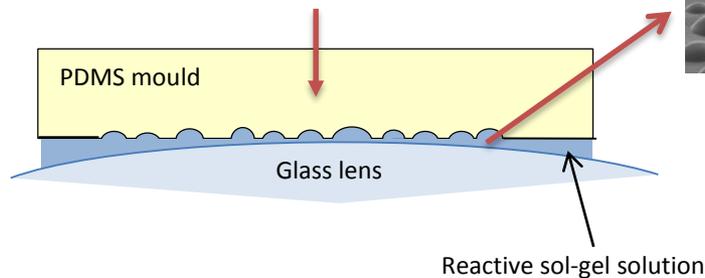


Size of the droplets

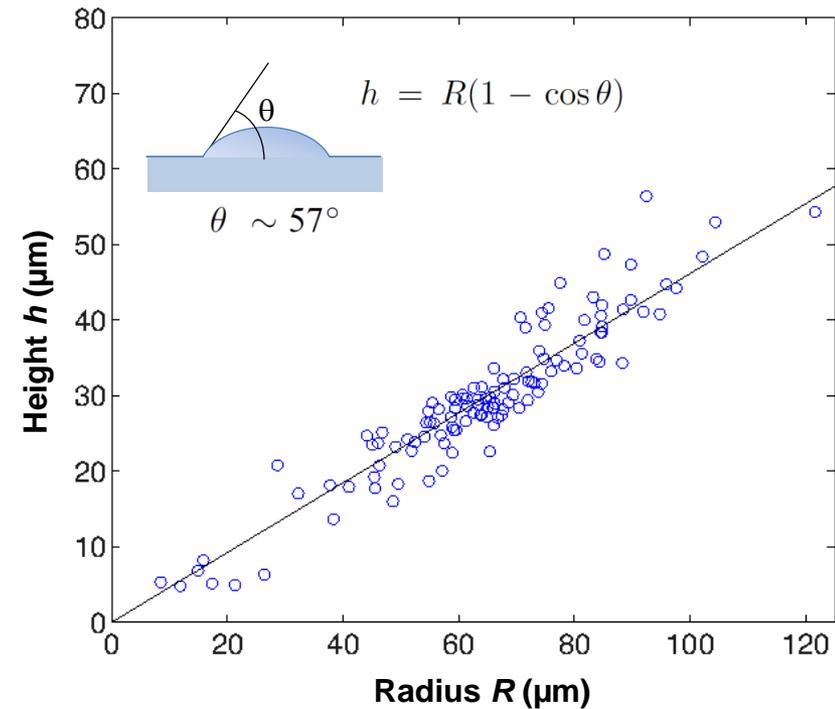
• 2. PDMS replica



• 3. Sol gel replica on a glass lens



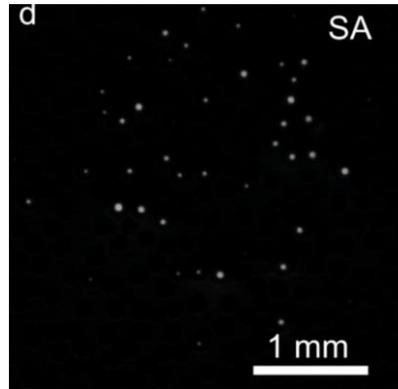
Shape of the asperities controlled by the contact angle



Contact devices

Contact imaging of micro-asperities contacts

- ✓ Contact radii & spatial distributions of micro-contacts (RA & SA surfaces)

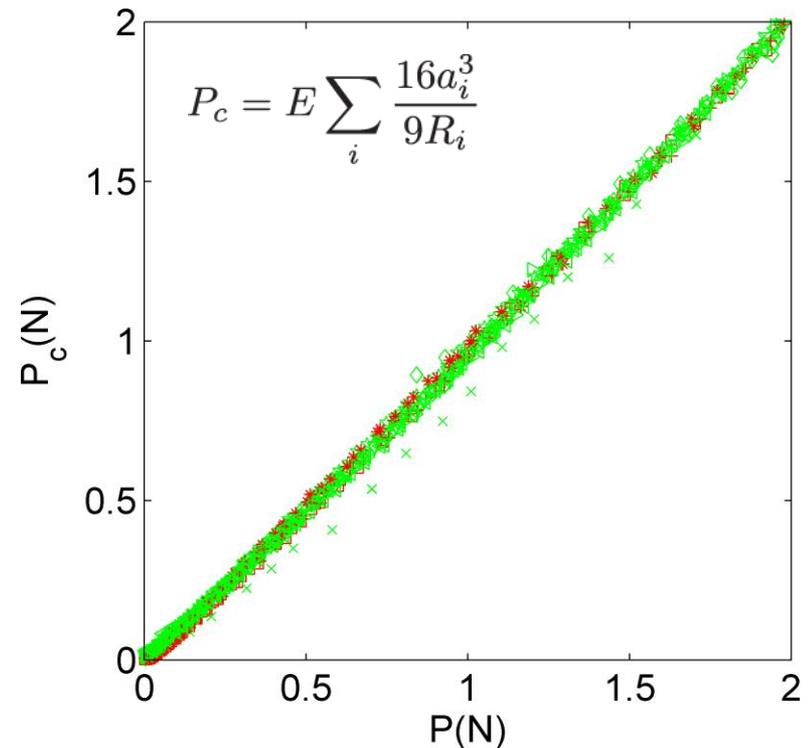
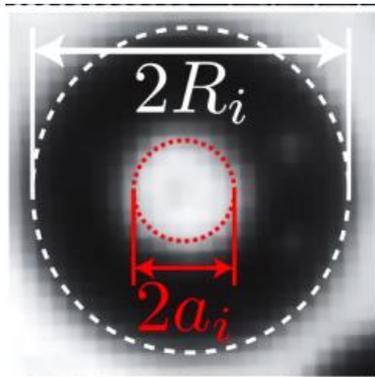


P=20 mN

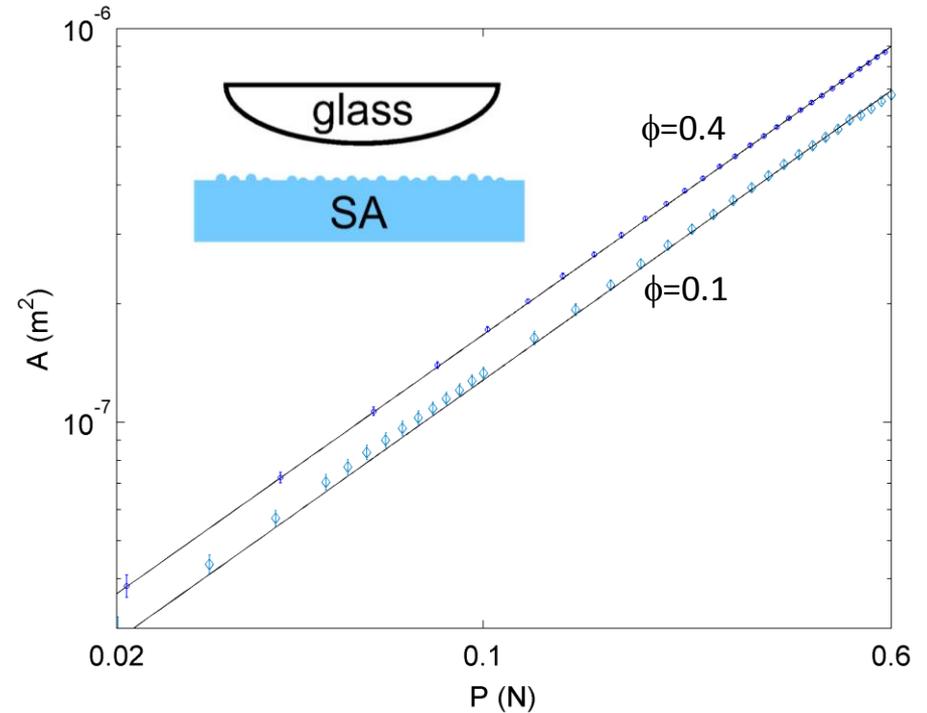
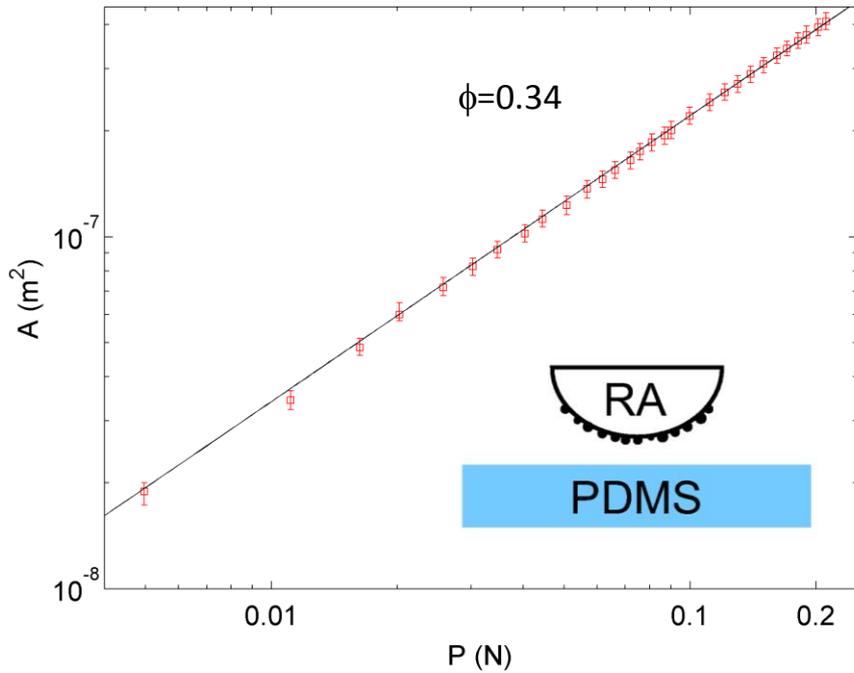
- ✓ Contact pressure distribution (RA surfaces only)

Hertz law assumed to be obeyed locally

$$P_i = \frac{16a_i^3}{9R_i}$$



Load dependence of the real contact area $A(P)$



Power law dependence $A \propto P^n$

RA surface $n=0.81 \pm 0.01$

SA surface $n=0.94 \pm 0.01$ independent of surface density of micro-asperities

A(P) relationship: role of elastic interactions ?

- Modified form of the GW model : Ciavarella's model
Ciavarella, 2008

Indentation depth of the i^{th} micro-asperity contact:

$$\delta_i = \delta_i^0 + \sum_{j \neq i}^N \alpha_{ij} \delta_j^{3/2},$$

Geometrical term

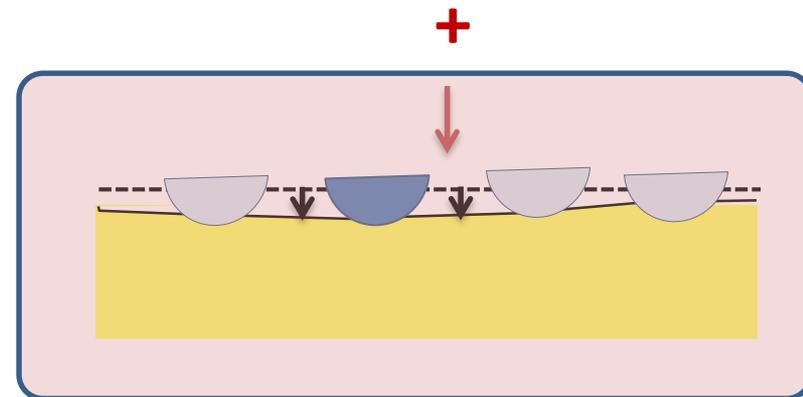
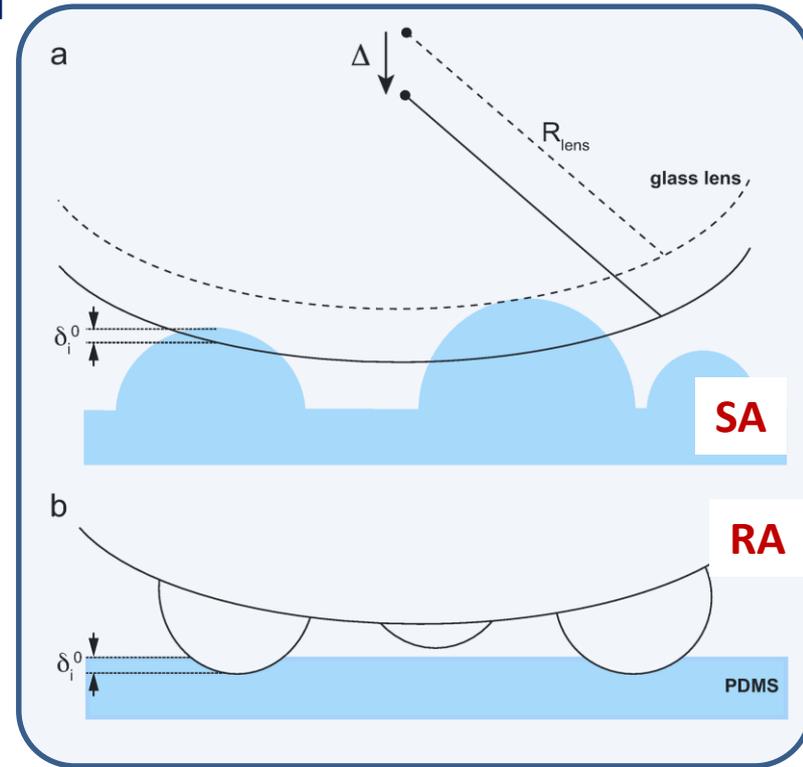
Elastic interaction term

→ With elastic interactions

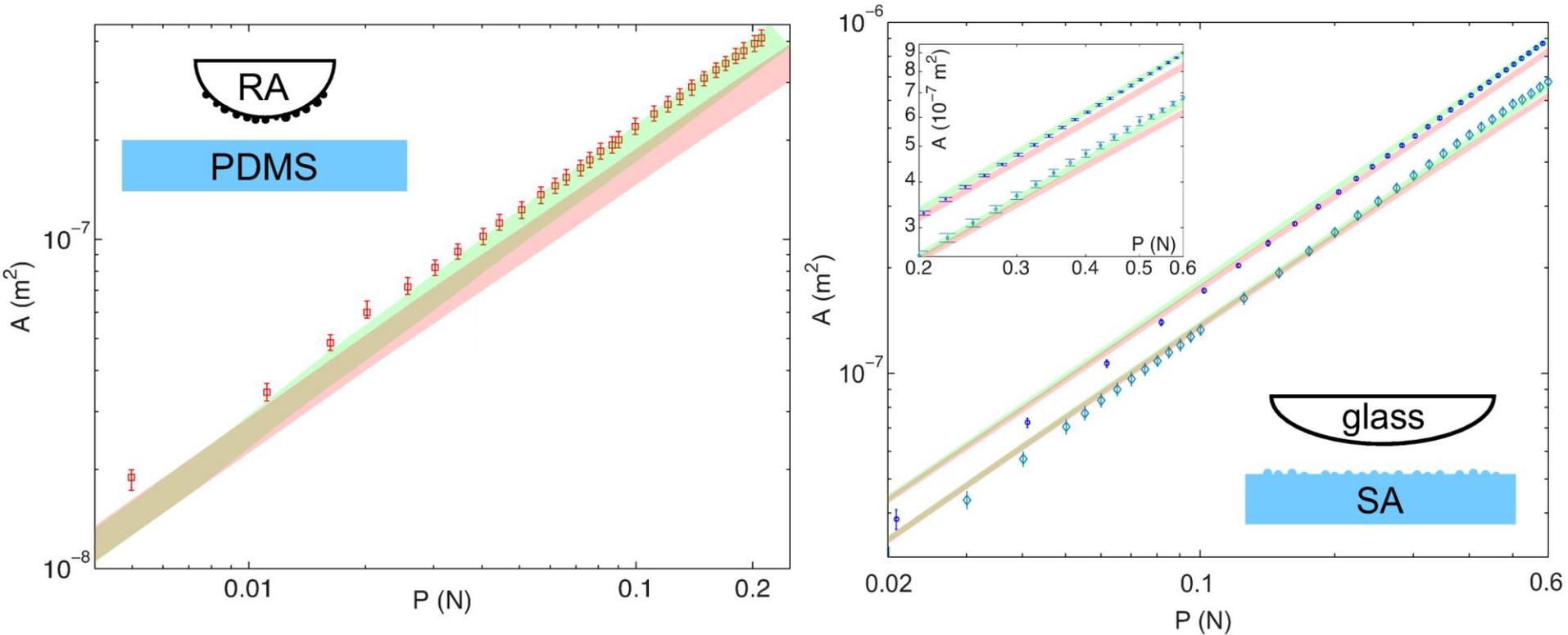
$$[\alpha_{ij}] = -\frac{4\sqrt{R_j}}{3\pi} \frac{1}{r_{ij}}, \quad i \neq j,$$

→ Without elastic interactions

$$[\alpha_{ij}] = 0$$



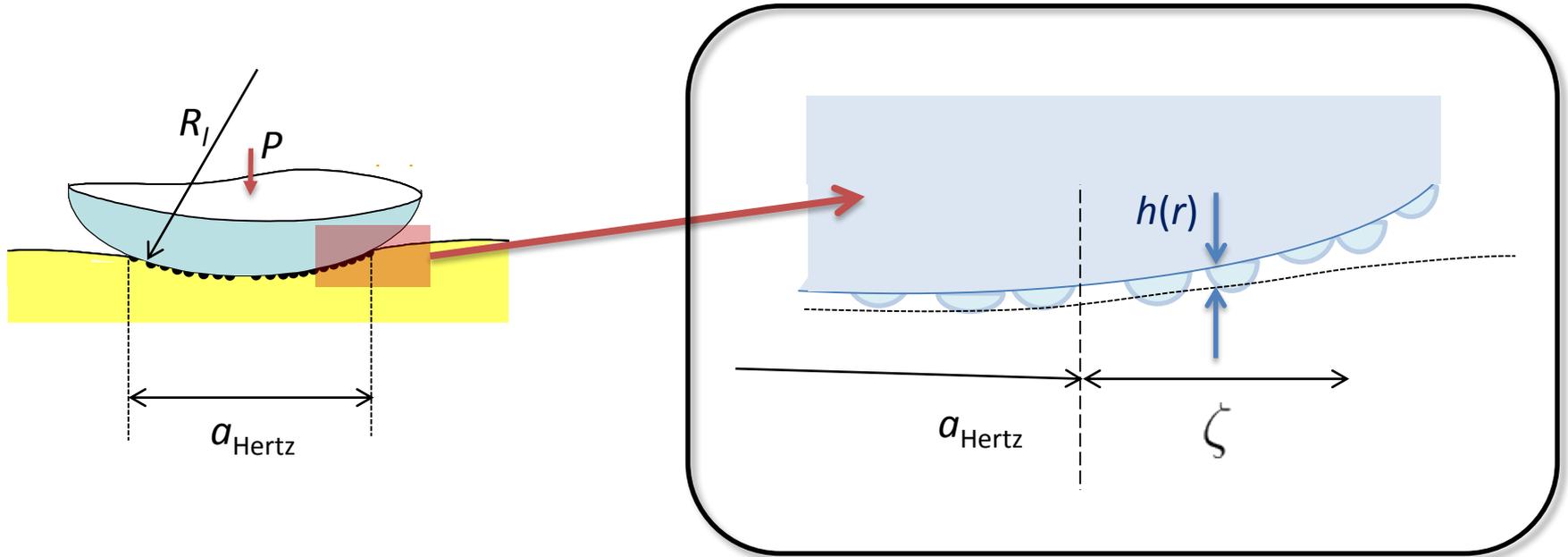
Calculated load dependence of the real contact area



-  With elastic interactions $[\alpha_{ij}] \neq 0$
-  Without elastic interaction $[\alpha_{ij}] = 0$

Departure of the A(P) relationship from linearity

- Lens curvature effect



Gap between the nominal ~ micro-asperity size →

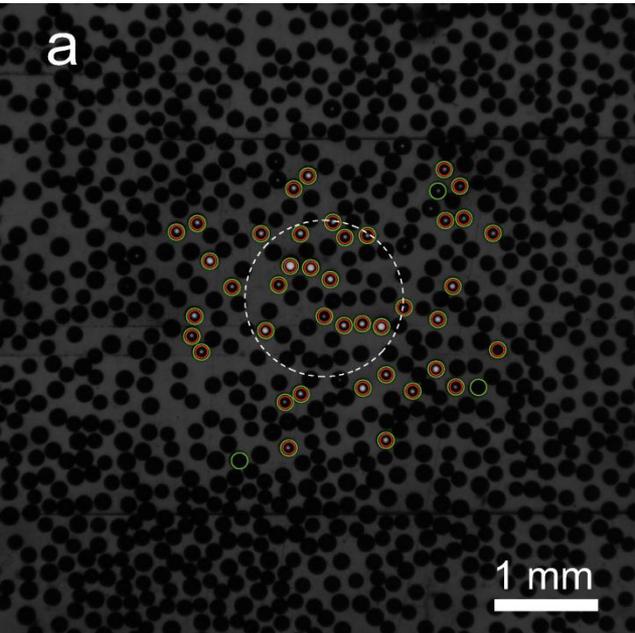
$$\zeta \propto P^{-1/9} R_l^{5/9}$$

$A \propto P^n$	RA surface	$R_l = 13 \text{ mm}$	$n = 0.81$
	SA surface	$R_l = 128 \text{ mm}$	$n = 0.94$

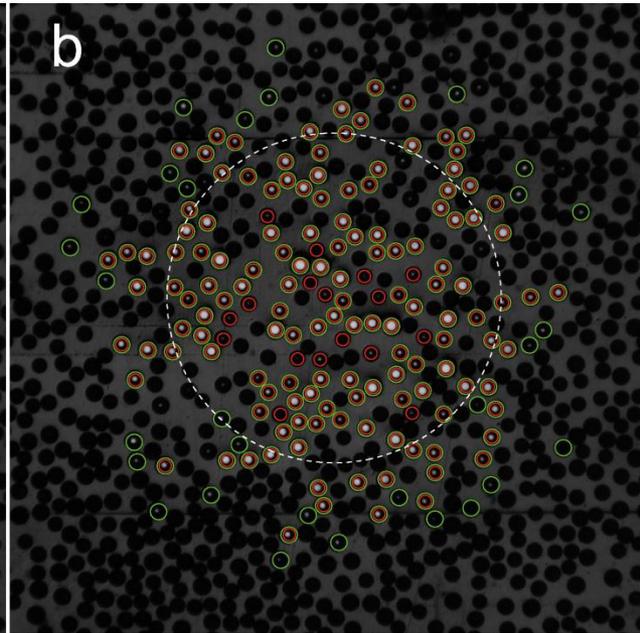
Micro-contacts spatial distributions

- SA Surface

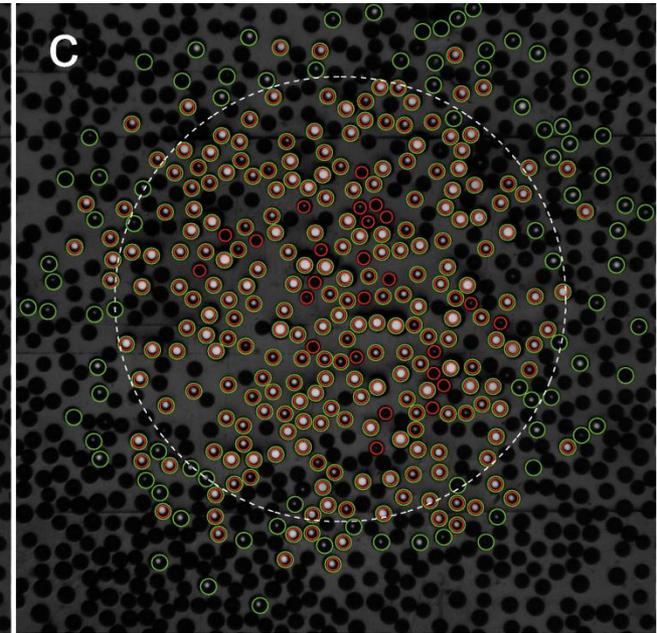
$P=0.02 N$



$P=0.2 N$



$P=0.5 N$



Predictions from Ciavarella's model

 $[\alpha_{ij}] \neq 0$

 $[\alpha_{ij}] = 0$

Contact pressure distribution $p(r)$

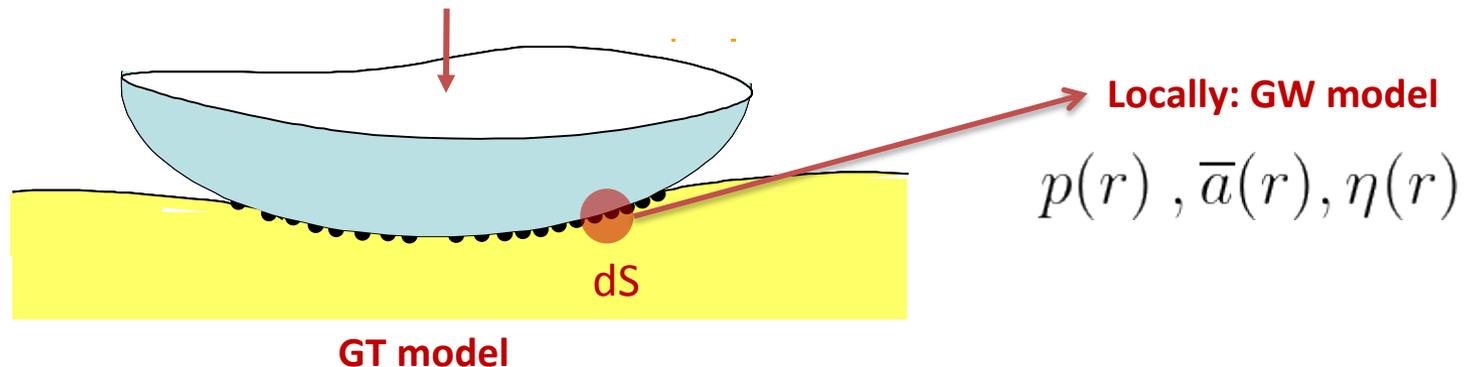
- **Experimentally** : summation of the local micro-contacts forces p_i within r and $r+dr$ (averaging over more than 20 realizations of the SA contacts)

- **Theoretically:**

- Ciavarella's model

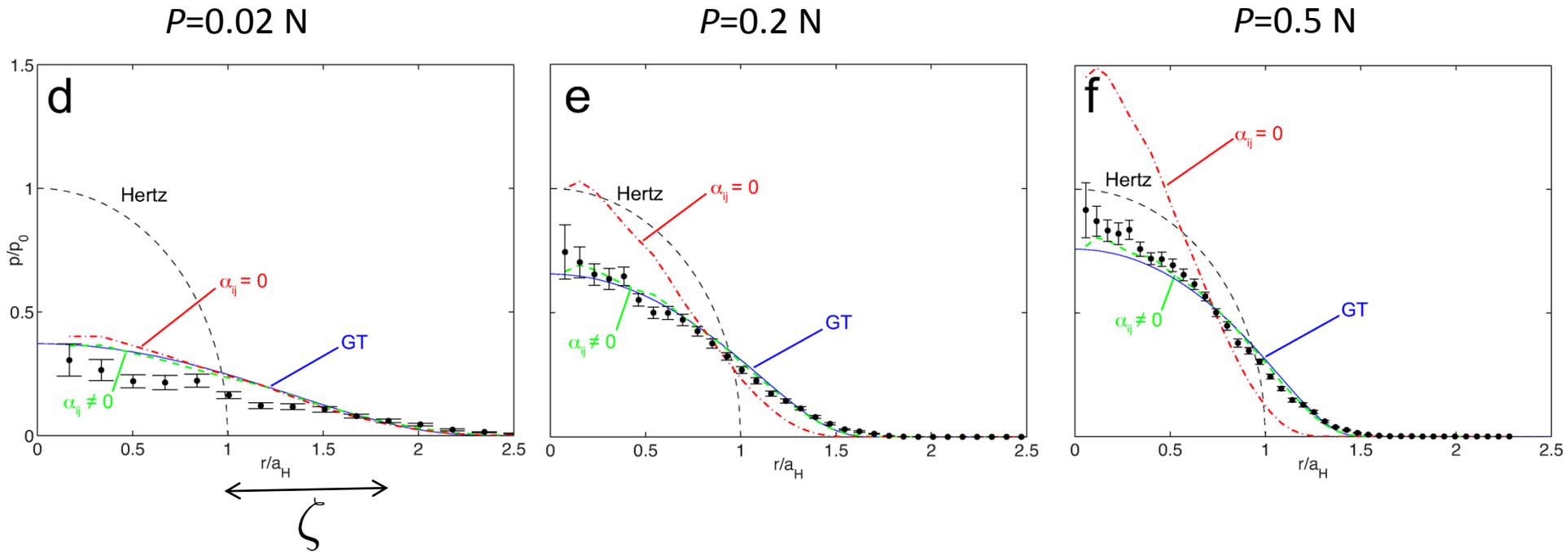
- **Extension of the GW model to the contact of rough spheres**

- Greenwood and Tripp (1967)



- **No short range elastic interaction** between neighboring micro-asperities
- **Long range elastic coupling** coming from the curvature of the nominal surfaces

Contact pressure profiles $p(r)$



- Added tail to the Hertzian pressure distribution $\zeta \propto R^{5/9} \sigma^{2/3} \sim \sqrt{R\sigma}$

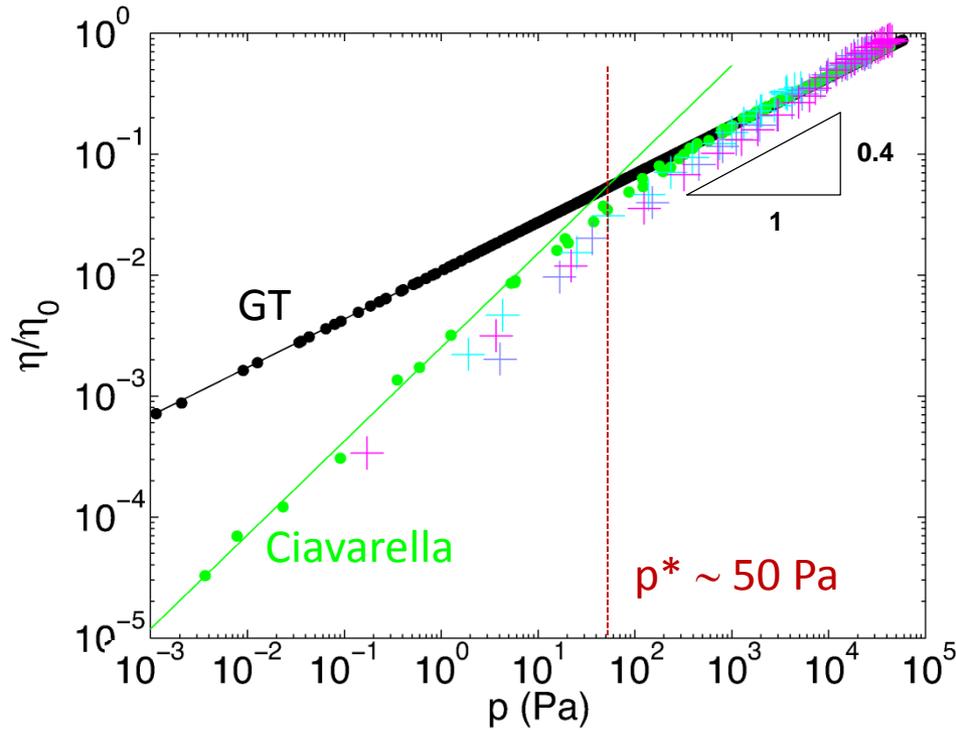
No significant difference between Ciavarella's and GT model



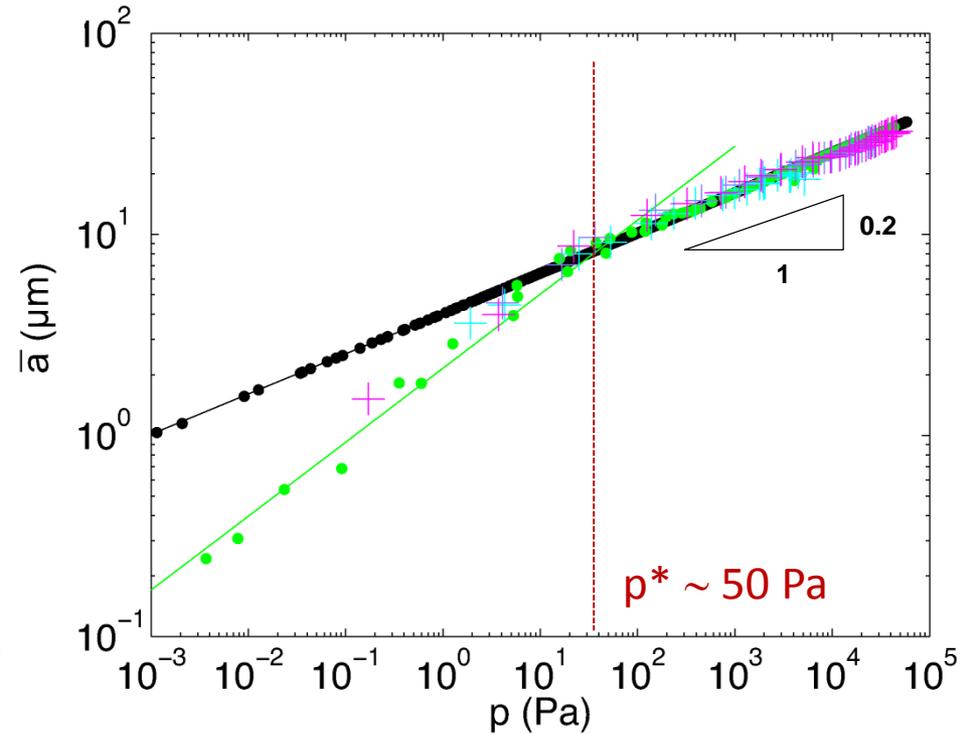
Short range elastic interactions does not affect the radial pressure distribution
 What about the distribution of quantities from which $p(r)$ derives?

Micro-contacts density and average micro-contact radius

Micro-contact density



Average micro-contact radius



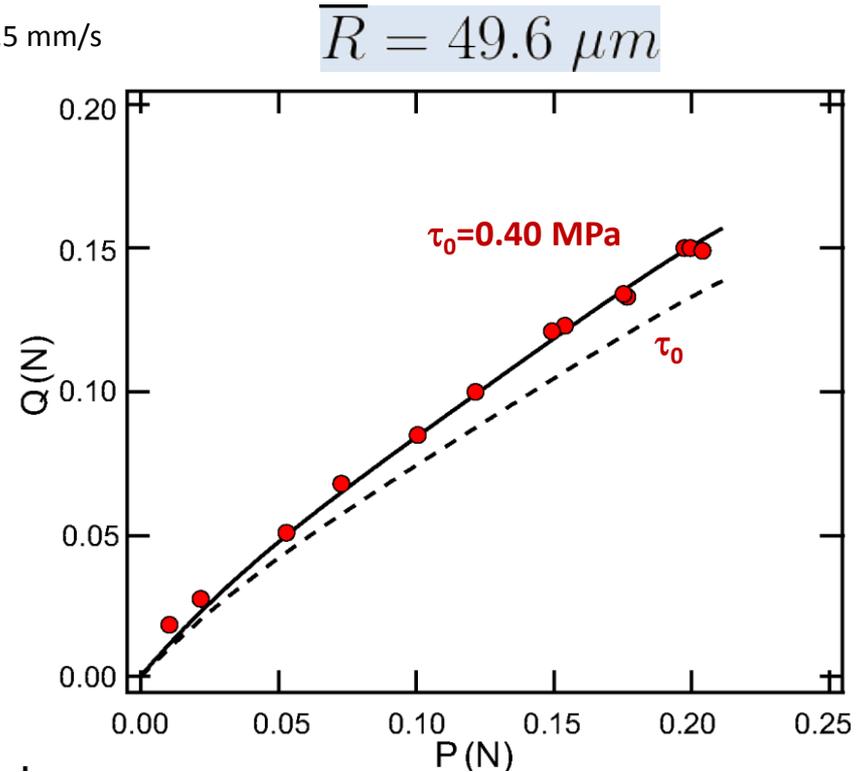
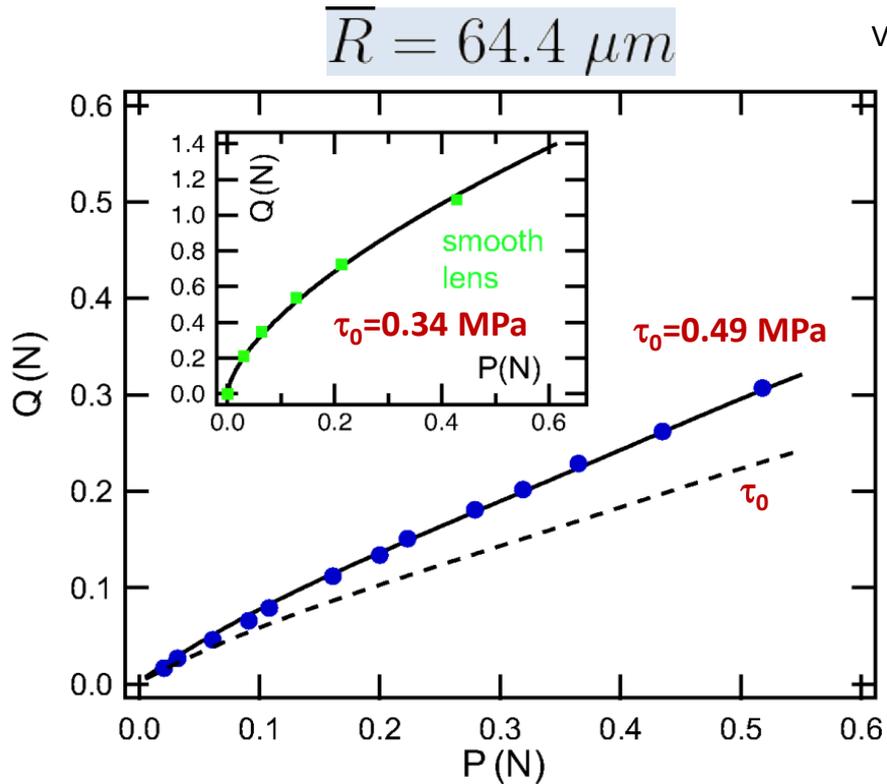
GW model for uniform random height distribution

$$\eta \propto p^{2/5}$$

$$\bar{a} \propto p^{1/5}$$

GW model obeyed over most of the contact pressure range

Frictional properties of RA surfaces



Smooth lens : $F = \tau_0 A$

τ_0 pressure independent

Patterned lens: $F \neq \tau_0 A$

with $A = \sum_i (\pi a_i^2)$

Interface shear stress cannot simply be transposed at all length scales

Conclusion / Outlook

- **Normal contact** of model randomly rough surfaces reminiscent to GW model
 - Long range elastic interactions coming from the curved profile of the indenter
 - Short range interactions between neighboring micro-contacts negligible

Experimental validation of the GW Williamson model

Extension to more realistic surface roughness including fractal surfaces ??

→ Experiments with hierarchical surface roughness

- Preliminary **friction** results show that frictional stress measured at macroscopic length scales cannot simply be transposed to multi-contact interfaces
 - Dependence of rubber friction on surface stretching ??