Frictional properties of contacts between a smooth viscoelastic rubber and rigid surfaces are investigated using a torsional contact configuration where a glass lens is continuously rotated on the rubber surface. From the inversion of the displacement field measured at the surface of the rubber, spatially resolved values of the steady state frictional shear stress are determined within the nonhomogeneous pressure and velocity fields of the contact. For contacts with a smooth lens, a velocity-dependent but pressure-independent local shear stress is retrieved from the inversion. On the other hand, the local shear stress is found to depend on both velocity and applied contact pressure when a randomly rough (sand-blasted) glass lens is rubbed against the rubber surface. As a result of changes in the density of microasperity contacts, the amount of light transmitted by the transparent multicontact interface is observed to vary locally as a function of both contact pressure and sliding velocity. Under the assumption that the intensity of light transmitted by the rough interface is proportional to the proportion of area into contact, it is found that the local frictional stress can be expressed experimentally as the product of a purely velocity-dependent term, \( k(v) \), by a term representing the pressure and velocity dependence of the actual contact area, \( A/A_0 \). A comparison between \( k(v) \) and the frictional shear stress of smooth contacts suggests that nanometer scale dissipative processes occurring at the interface predominate over viscoelastic dissipation at microasperity scale.

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I. INTRODUCTION

Rubber friction is a topic of huge practical importance in many applications, such as tires, rubber seals, conveyor belts, and syringes, to mention only a few. However, there is an incomplete understanding of the parameters that control the frictional behavior of rubber surfaces. Since the seminal experimental work by Grosh [1], rubber friction is usually assumed to involve two dissipative components. The first one, often denoted as the adhesive component, corresponds to thermally and stress activated pinning and depinning mechanisms between rubber molecules and the contacting surface. This idea forms the basis of the Schallamach model [2], which was subsequently extended by Chernyak and Leonov [3]. In a later study, Vorvokalos and Chaudhury [4] also showed that these models can consistently be used to describe the dependence of friction of poly(dimethylsiloxane) (PDMS) elastomers on molecular parameters such as molecular weight. The second dissipative component involved in rubber friction is assumed to correspond to viscoelastic losses associated with the contact deformation of the soft rubber. In the case of a hard, rough surface sliding on a viscoelastic rubber, viscoelastic losses at microasperity scale occur at characteristic frequency of the order of \( v/d \) where \( v \) is the sliding velocity and \( d \) is a characteristic size of asperity contacts. This so-called hysteretic component of friction was first evidenced by Greenwood and Tabor [5] in a series of experiments, in which hard spheres and cones were sliding or rolling on well-lubricated rubber surfaces. The work by Grosh [1] extended these investigations to the more complex situation of rubber sliding on microscopically rough surfaces. A maximum in friction was found to occur at a sliding velocity related to the frequency with which the asperities of the rough surface deform the rubber surface. This maximum was absent on a smooth track, thus reflecting the deformation losses induced by the passage of the asperities over the rubber surface. These frictional mechanisms involving viscoelastic losses at microasperity scale have motivated the development of several theoretical models starting from Fourier transform analysis applied to periodic surfaces [6,7] to the more complex model developed by Persson for rubber friction on randomly rough surfaces [8,9]. Using a spectral description of the topography of the rough surfaces, Persson’s theory predicts how the component of friction force associated with hysteretic losses varies with velocity and contact pressure from an estimate of the actual contact area. Some experimental results tend to support this theory [10], but a detailed examination of the effects of surface topography on rubber friction remains very challenging in the case of randomly rough surfaces where adhesive and hysteretic components are strongly intricate.

In a previous work [11], we have investigated the friction of a PDMS rubber with model rough surfaces consisting of silica lenses covered with various densities of spherical colloidal nanoparticles. From an examination of the pressure dependence of the frictional shear stress, we showed that the actual contact area was close to saturation in the whole range of applied contact load and sliding velocity. These model surfaces thus allowed quantifying the contributions of interface dissipation and hysteretic losses to friction without the complications arising from the pressure and velocity dependence of the actual contact area. In addition, the use of a monodisperse distribution of colloidal particles allowed to control both the characteristic frequency associated with deformation at asperity scale and the volume of the viscoelastic substrate that is affected by this deformation. Within this framework, we were able to determine experimentally the hysteretic component of friction which compares well with theoretical calculations. In this study we consider the more realistic situation of a viscoelastic rubber sliding against a
randomly rough rigid surface where the proportion of area into contact is expected to depend on both the applied pressure and the sliding velocity. Experiments are carried out using a torsional contact configuration which, as explained below, allows investigating frictional energy dissipation at the interface without the complications arising from bulk viscoelastic losses at the scale of the macroscopic contact. In addition, the inversion of the measured displacement field at the surface of the rubber provides local values of the frictional shear stress within the nonhomogeneous pressure and sliding velocity fields of the contact. Local changes in the density of asperity microcontacts are evidenced from a measurement of the amount of light transmitted through the transparent rough contact.

In the first part of this paper, we consider the case of a smooth contact where friction is likely to arise only from molecular scale dissipation at the intimate contact formed between the surfaces. In the second part, we examine the pressure and velocity dependence of the frictional shear stress within rough contacts where asperity scale viscoelastic losses are likely to come into play. We show that the measured shear stress can be expressed as the product of a velocity- and pressure-dependent term which describes the changes in the actual contact area as a function of nominal contact pressure and sliding velocity. From a comparison between the smooth and rough contacts, we discuss in a last part the contributions of interface dissipation and hysteretic losses to friction.

II. EXPERIMENTAL DETAILS

A. Materials and sample preparation

As a substrate, we use an epoxy-based rubber obtained by crosslinking diglycidyl ether of bisphenol A (DER 332, \(M_w = 340\text{ g mol}^{-1}\), Dow Corning) with a polyether-diamine crosslinker (Jeffamine\textsuperscript{©} ED2003, \(M_w = 2003\text{ g mol}^{-1}\), Huntsman Chemical). As detailed in Appendix A, this rubber exhibits a significant change (about one order in magnitude) in the loss modulus in the characteristic frequency range \((\approx 0.1–10^3\text{ Hz})\) involved in surface deformation at microscale. In order to elaborate the specimens, each of the reactive parts is first separately stirred in a silicone bath at 70°C for about 30 min. Then epoxy is mixed with the stoichiometric amount of diamine determined with the epoxy-equivalent weight and amine hydrogen equivalent weight given by the supplier (Jeffamine\textsuperscript{©} Data Sheets). The reactive mixture is stirred and subsequently degassed for about 40 min at 50°C in a vacuum chamber. Then the mixture is poured into a parallelepiped-shaped PDMS mold (size: \(4.5\text{ cm} \times 4.5\text{ cm} \times 1.5\text{ cm}\)) and cured at 120°C for 20 h. In order to monitor contact induced surface displacements, a square network of small cylindrical holes (dia. \(10\mu\text{m}\), depth \(2\mu\text{m}\) and center-to-center spacing \(70\mu\text{m}\)) is stamped on the PDMS surface. Once imaged in transmission with a white light, the pattern appears as a network of dark points. This surface marking is simply achieved by patterning the bottom part of the PDMS mold by a network of cylindrical posts using conventional soft lithography techniques. After curing, the glass transition temperature of the epoxy rubber is \(-42^{\circ}\text{C},\) as determined by differential scanning calorimetry (DSC) at a scan rate of \(10^{\circ}\text{C min}^{-1}\).

During friction experiments, the rubber specimen is contacting a plano-convex BK7 glass lens (Melles Griott, France) with a radius of curvature of 14.8 mm. After cleaning, the root-mean-square roughness of the lens is less than 2 nm, as measured by AFM using \(1 \times 1\mu\text{m}^2\) pictures. One of the lenses is rendered microscopically rough using sand blasting (average grain size of 60 \(\mu\text{m}\)). The topography of the surface has been characterized by AFM measurements using image sizes ranging from \(50 \times 50\mu\text{m}^2\) to \(500 \times 500\mu\text{m}^2\). Figure 1 depicts the results in the form of a roughness power spectrum density (PSD) \(C_r(q)\). This PSD decays according to a power law, from \(50\mu\text{m}\) down to the nanometer scale. Accordingly, the surface roughness can be defined as a self-affine fractal \([C_r(q) \propto q^{-2d_f+1}]\) with a Hurst exponent \(H = 0.58\) and a fractal dimension \(D_f = 3 - H = 2.42\). The root-mean-square roughness of the sand-blasted surface is measured as \(1.69 \pm 0.19\mu\text{m}\) using \(50 \times 50\mu\text{m}^2\) images.

B. Friction setup and contact imaging

Contact torsion experiments are carried out using a custom-made device which is fully described in Ref. [12]. The experiments consist in rotating continuously a glass lens about an axis perpendicular to the surface of the rubber substrate and passing through the apex of the lens. Normal contact is achieved under an imposed indentation depth condition (between 60 and \(320\mu\text{m}\)) by means of a linear displacement stage. The resulting contact radius lies in the range \(0.3–2.2\text{ mm}\). Specimen size \((4.5\text{ cm} \times 4.5\text{ cm} \times 1.5\text{ cm})\) ensures that the ratio of the substrate thickness to the contact radius is greater than 10, i.e., that semi-infinite contact conditions are achieved during torsion experiments [13]. Separate indentation
FIG. 2. Schematic description of the parallel light system used to illuminate the contact region. (a) optical fiber light; (b) microscope objective; (c) pinhole; (d) convex lens; (e) contact lens; (f) rubber specimen; (g) CMOS camera.

experiments using the same device equipped with a load cell allowed to determine the relationship between indentation depth and normal load (the load cell has to be removed during torsional contact experiments for imaging purposes). During friction experiments, the glass lens is rotated at imposed angular velocity between 0.01° and 10° s⁻¹ using a motorized rotation stage. Prior to use, the lenses are successively cleaned with acetone and ethanol in an ultrasonic bath for about 5 min. Epoxy-based specimens are thoroughly washed with 2-isopropanol and subsequently dried under vacuum.

During torsion, images of the contact zone are continuously recorded through the transparent rubber substrate using a zoom lens and a CMOS camera. The system is configured to a frame size of 1024 × 1024 pixels with 8 bits resolution. Images are acquired at a frequency ranging from 0.01 to 30 Hz. The contact zone is illuminated using a parallel light system located behind the glass lens, as schematically described in Fig. 2. In the case of the smooth contact interface, subpixel detection of individual markers on the epoxy surface is carried out directly from single images taken during steady state friction [as that shown in Fig. 3(a)] using a particle tracking method. Each contact picture provides a displacement field with about 6000 data points with a spatial resolution corresponding to distance between markers (i.e., 70 µm). In the case of rough interfaces, the contact appears as bright spots against a darker background as a result of light scattering by the roughened surface [Fig. 3(b)]. It is therefore no longer possible to detect the markers on the rubber surface on a single image. However, an averaging procedure allows revealing the location of the markers under steady state friction. As shown in Fig. 3(c), averaging several images taken during steady state friction suppresses nearly all the light intensity fluctuations induced by surface roughness, thus allowing us to reveal the location of the markers which are fixed with respect to the camera.

III. FRICTION OF SMOOTH CONTACTS

When the smooth lens is twisted starting from rest, a stiction stage is first encountered which corresponds to the shear failure of the adhesive contact. This stiction process occurs according to a fracture-like process characterized by progressive slip propagation from the periphery to the center of the contact. This phenomenon was discussed in a previous study [12], and it will not be considered further in this paper. In the case of the investigated epoxy rubber, this transient stiction phenomenon occurs for twist angles θ ≤ 50° for all indentation depths and angular velocities under consideration.

FIG. 3. Contact pictures taken during steady state friction. (a) smooth contact; (b) rough contact; (c) rough contact after image averaging. Averaging allows suppressing most of the light intensity fluctuations due to the rotating rough surface. The dot lattice on the rubber surface then becomes apparent.
Then a steady state friction state is achieved as indicated by the time independence of markers location on the rubber surface. As an example, Fig. 4 depicts the displacement of an individual marker located within the contact as a function of the applied twist angle. Owing to the symmetry of the contact, this displacement is expressed using its cylindrical components with respect to the center of rotation (only the azimuthal displacement component $u_\theta$ is reported in the figure as the radial displacement component $u_r$ is found to be systematically negligible in all experiments). After an initial increase corresponding to the stiction stage ($\theta \lesssim 40^\circ$), a steady state is achieved. Here the time-independent location of the marker is indicative of the achievement of a vanishing strain rate within the bulk rubber substrate. This means that no significant relaxation process takes place at the scale of the contact within the considered time window. The bulk substrate can thus be considered as deformed in a relaxed, time-independent, state.

Figure 5 shows a typical displacement field obtained with the smooth contact under such a steady state friction condition. From this measured displacement field, the corresponding contact stress distribution can be retrieved using an appropriate inversion procedure. In a previous study dealing with linear sliding of silicone rubbers [14], we showed that an inversion method based on a linear elastic contact mechanics approach can be inaccurate due to the occurrence of finite strains at the edge of the contact. A finite elements (FE) inversion procedure was thus developed in order to handle the associated geometrical and material nonlinearities. Here a calculation of the surface shear strain $\epsilon_{r\theta} = 1/2(\partial u_\theta / \partial r - u_\theta / r)$ from the measured azimuthal displacement profiles (bottom part of Fig. 5) shows that strains as high as 0.3 are achieved at the vicinity of the contact edge, which are also outside the linear range of the epoxy rubber (about 0.1). In order to evaluate the effects of these nonlinearities on the inversion, a displacement field was inverted using either a linear elastic approach based on Green’s tensor or a FE method able to handle the geometrical and material nonlinearities of the problem. The results reported in Appendix B show that both approaches give the same result. It therefore turns out that finite strains do not induce any significant error in a linear elastic inversion of torsional displacement, which can be justified by some theoretical considerations [15]. As a result, all the stress fields to be reported in this study have been obtained from the semianalytical deconvolution of the measured displacement fields using the Green’s tensor approach fully detailed in Ref. [16].

The surface shear stress distribution of the smooth contact interface was systematically determined from the inversion of the measured steady state azimuthal displacements at various indentation depths and angular velocities. All the shear stress data obtained from the inversion are expressed...
in a nondimensional form, $\bar{\tau}(r) = \tau_0(r)/E_r$, where $E_r$ is the relaxed elastic modulus of the rubber. As shown in Fig. 6(a), a nearly constant frictional shear stress is achieved within the contact zone except at the center of the contact where shear stress vanishes for symmetry reasons. Contact pressure being expected to decrease continuously along the contact radial coordinate, it turns out that frictional shear stress is pressure independent, as already reported for smooth glass-PDMS contacts [12,16]. A close examination of stress profiles obtained at various imposed velocities [Fig. 6(b)] shows a systematic positive gradient along the radial coordinate, which should reflect the velocity dependence of the interface shear stress. This assumption was further considered from a plot of the measured local shear stress values as a function of the local sliding velocity $v = \theta r$, where $\theta$ is the angular velocity and $r$ is the radial coordinate. According to a previous investigation [12], the transition to a vanishing frictional stress in the vicinity of the contact center occurs over a length scale which represents about 10% of the contact radius and which is essentially dictated by the cutoff frequency of the deconvolution operation. As a result, data points close to the center of the contact ($r/a < 0.1$ where $a$ the contact radius) were discarded from the analysis together with data points outside the contact area ($r/a > 1$). As shown in Fig. 7, all the selected shear stress values merge on a single master curve when the applied angular velocity is varied. Over nearly three orders of magnitude in the sliding velocity, the shear stress is observed to increase continuously by about a factor three. The shear stress being measured in a steady state friction regime where no displacement occurs at the macroscale, it is thus associated with small-scale dissipative processes. For such a smooth and intimate contact, friction is usually considered to arise from molecular scale dissipative processes occurring at the sliding interface. As mentioned in the Introduction, formation and breakage of adhesive molecular bonds at the contact interface is often invoked as the underlying physical mechanism [2,3]. For rubber sliding on optically smooth glass, Grosh [1] noted that the velocity corresponding to maximum friction and the frequency corresponding to maximum viscoelastic loss form a ratio that is on the order of 7 nm for various materials. This nanometric length scale was assumed by Grosh to represent the scale of microasperity contacts within the rough contact interface. Here the available frequency and sliding velocity ranges do not allow to extract a very accurate value of this characteristic length scale. However, it can be seen in Fig. 7 that the shape of the $\bar{\tau}(v)$ plot matches that of the loss component of the shear modulus, $G''$, when the latter is represented as a function of $\lambda \omega$, where $\omega$ is the frequency and $\lambda$ is a characteristic length close to 6 nm. In the following section, we address frictional dissipative processes occurring at larger length scales, i.e., at the scale of microasperity contacts within the rough contact interface.
but also potentially on the local sliding velocity as a result of viscoelastic effects. In the following section, the changes in the density of microcontacts as a function of local pressure and velocity are further considered from an examination of fluctuations in the light transmitted by the transparent rough contacts.

B. Optical transmissivity of the multicontact interface

Some interesting features of the rough contacts emerge when the changes in the light transmitted locally by the interface are considered. As mentioned above, rough contacts appear as spatially heterogeneous as a result of the scattering nature of the glass surface [cf. Fig. 3(b)]. Because of the difference between the index of refraction of the solids and that of the air, the rough interface transmits light more efficiently when the surfaces are in intimate contact than when they are out of contact. No complete optical model is available to describe these effects, but, as a first approach, one can neglect scattering and just consider light transmission in contact and noncontact regions of the rough interface. Obviously, light transmission will be more efficient if only one interface is present (contact condition) instead of two (noncontact condition). Accordingly, the intensity of transmitted light at a given location within the rough contact should carry information about the actual area of microasperity contacts. Such an idea was initially developed by Dietrich and Kilgore [17,18] in a study where the actual contact area between rough transparent materials was determined from microscope contact observations. The relevance of this approach to rough contacts interfaces involving polymers was subsequently demonstrated in later studies by Scheibert et al. [19], Rubinstein and co-workers [20], and Krick et al. [21]. As discussed by Dietrich and Kilgore, the analysis of the images can be complicated by various optical scattering and resolution effects (especially at the edges of microcontacts), which requires appropriate deconvolution procedures if one wants to get a quantitative measurement of the actual contact area from contact images. Here contact images will be analyzed under the assumption that transmitted light intensity at a given contact location is proportional to the proportion of area into contact. As detailed below, the validity of this assumption is supported by static indentation experiments carried out at various imposed indentation depths. In order to improve the ratio to noise ratio of the camera, each static contact image at a given prescribed indentation depth is obtained by averaging 300 images. A reference image is also obtained in the same way using a noncontact configuration. When subtracted to the contact image, this reference image enforces the background of the image to be almost zero thus allowing to clearly identify the size of the circular contact region. For each pixel, a normalized transmitted light intensity \( I_n \) is defined as

\[
I_n = \frac{I_c - I_r}{I_r},
\]

where \( I_c \) is the measured light intensity under contact conditions and \( I_r \) is the corresponding intensity in the reference image (without contact). Here it should be kept in mind that the transmitted light intensity measured at the length scale of a pixel (\( 5 \times 5 \mu m^2 \)) is characteristic of a multicontact interface as a result of the self-affine fractal nature of the glass surface.
Normalized radial intensity profiles are subsequently obtained from an angular average of the normalized images with respect to an origin defined by the apex of the lens. Results are shown in Fig. 9(a) where the profiles can be seen to be shifted to higher light intensity values when indentation depth is increased. Interestingly, it comes out that all the profiles obtained at various contact loads collapse onto a single plot [Fig. 9(b)] when intensity data are normalized with respect to the average contact pressure $p_m = P/\pi a^2$ and the contact radius $a$, respectively ($P$ is applied normal load).

Normalized radial intensity profiles are obtained at increasing applied indentation depth (from 20 to 300 μm by 20 μm steps, from bottom to top). (b) Reduced profiles obtained by dividing the normalized intensity and the radial coordinate by the average pressure $p_m = P/\pi a^2$ and the contact radius $a$, respectively ($P$ is applied normal load).

FIG. 9. (Color online) Transmitted light intensity during static indentation experiments. (a) Normalized intensity profiles obtained at increasing applied indentation depth (from 20 to 300 μm by 20 μm steps, from bottom to top). (b) Reduced profiles obtained by dividing the normalized intensity and the radial coordinate by the average pressure $p_m = P/\pi a^2$ and the contact radius $a$, respectively ($P$ is applied normal load).

FIG. 10. Integrated normalized light intensity transmitted through the rough contact as a function of normal load (static indentation).
the measured local shear stress can thus be expressed as
\[
\tau(p,v) = k(v)I_0(p,v) \propto k(v)A(p,v)/A_0.
\] (2)

V. DISCUSSION

From the inversion of the displacement field at the surface of a viscoelastic rubber contacting a rigid spherical asperity, local values of the steady state frictional shear stress were determined under torsional contact conditions. For rough contacts, measured values of the local shear stress are representative of a multicontact interface under given sliding velocity and nominal contact pressure conditions. In addition, information about the local proportion of area into contact \( A/A_0 \) is provided from contact images under the assumption that optical transmittivity of the rough interface is proportional to \( A/A_0 \). As detailed above, this assumption is supported by separate static indentation measurements where it yields the expected linear relationship between the actual contact area and the applied nominal contact pressure. From a systematic investigation of the local shear stress and transmitted light intensity as a function of the applied indentation depth and twisting rate, it is found experimentally that the frictional shear stress can be expressed as the product of two terms [cf. Eq. (2)]. The first one, \( A/A_0 \), incorporates the velocity and pressure dependence of the microcontacts density. The second one is a pressure-independent term, \( k(v) \), which can be viewed as some averaged measurement of the amount of frictional energy dissipated within microcontacts. In other words, \( A/A_0 \) corresponds to a contact mechanics term describing the density of microcontacts under steady state sliding while \( k(v) \) quantifies the dissipative processes at play within asperity microcontacts.

As shown by the dotted line in Fig. 12, it can interestingly be noted that the magnitude of \( k(v) \) is similar to that of the frictional shear stress measured for smooth contacts and that it follows a very similar velocity dependence. This suggests that frictional energy dissipation within microasperity contacts is mostly due to interfacial dissipation, the contribution of viscoelastic losses at asperity scale being negligible. This statement can be further considered within the framework of the friction model detailed in the introduction. Accordingly, the frictional force is assumed to arise from two independent contributions, namely, the so-called adhesive and hysteric components. The so-called adhesive term encompasses all dissipative mechanisms occurring at the points of intimate contact between the solids, i.e., on length scales lower than asperity size. The hysteretic term corresponds to the force required to displace the rubber material from the front of the rigid asperities. Here, it represents the contribution of the viscoelastic losses involved in the deformation of the rubber substrate by microasperities. Rewritten in terms of shear stress, this model can be expressed as

\[
\tau = \tau_a + \tau_h,
\] (3)

where \( \tau_a \) and \( \tau_h \) are respectively the adhesive and hysteretic terms. The adhesive term can simply be expressed as

\[
\tau_a = \tau_0 A/A_0,
\] (4)

where \( \tau_0 \) is the frictional shear stress of the smooth contact interface.
An exact calculation of the hysteretic component $\tau_h$ is much more complicated as it implies to solve the viscoelastic contact problem taking into account the whole frequency distribution associated with the topography of the self affine rough surface. As a first order approximation, we follow a simple approach where the rough surface is assimilated to a distribution of identical, noninteracting, spherical asperities. Following a calculation by Greenwood and Tabor [5], the friction force at the scale of a single asperity can be expressed as

$$F_{asp} = \alpha \frac{E_{eff} a^4}{4 R^2},$$

where $R$ is the radius of curvature of theasperity and $E_{eff}$ is a frequency-dependent effective modulus defined as

$$E_{eff}(\omega) = \frac{|E(\omega)|}{1 - \nu^2},$$

where $\omega$ is a characteristic frequency defined as $\omega = v/a$ and $\nu$ is the Poisson’s ratio whose variations with frequency are neglected. In the above equation, $\alpha$ is term representing the fraction of the input elastic energy which is lost as a result of viscoelastic dissipation. The hysteretic frictional stress can thus be written as $\tau_h = \phi F_{asp}$ where $\phi$ denotes the surface density of asperities. $\phi = A/(\pi a^2 A_0)$ thus allowing us to express $\tau_h$ as

$$\tau_h = \alpha \frac{E_{eff} A}{4\pi A_0} \left( \frac{a}{R} \right)^2.$$  

As an upper bound value for $\tau_h$, one can take $a \approx R$, which gives

$$\tau_h \approx \alpha \frac{E_{eff} A}{4\pi A_0}.$$ 

From Eqs. (4) and (8), the total frictional stress within the rough interface can thus be expressed as

$$\tau = \frac{A}{A_0} \left( \tau_0 + \alpha \frac{E_{eff}}{4\pi} \right).$$

Within the investigated sliding velocity range (0.1 to 100 $\mu$m s$^{-1}$), the adhesive term $\tau_0$ is found to vary between 0.2 and 0.5 MPa (Fig. 7). The estimate of the second, viscoelastic term, in the right-hand side of Eq. (9) requires a knowledge of the dissipation factor $\alpha$. Following an exact viscoelastic calculation by Persson [26], we take for $\alpha$ an asymptotic (low velocity) value calculated as $\alpha \approx 5 \tan \delta$ where $\tan \delta$ is the loss tangent of the rubber substrate. Using this approach and the viscoelastic data reported in the Appendix, the viscoelastic tangent of the rubber substrate. Using this approach and the velocity) value calculated as

$$\nu$$

is the Poisson’s ratio whose variations with frequency are
domestic to consist

to the hysteretic component to friction would require that the multiscale features of surface topography as well as nonlinear effects encountered during deformation at microasperity scale are accounted for. Some of these features are embedded within theoretical rough contact models such as that developed by Persson [9], but using these models would require extensive calculations which are beyond the scope of this study. From an experimental perspective, more insights into the adhesive and hysteretic components to friction could be gained from experiments where the physical chemistry of the glass surface is varied (using silanization, for example) independently of the viscoelastic properties of the rubber or, conversely, where the viscoelasticity of the substrate is changed independently of the properties of the glass surface. When doing so, one should take care to the potential occurrence of stick-slip motions or friction instabilities which would preclude such an analysis.

VI. CONCLUSION

Using contact imaging approaches, we were able to determine the distribution of frictional stresses withincontacts between a smooth viscoelastic rubber and a rigid rotating lens. When the lens surface is made randomly rough, the local frictional stress is observed to be dependent on both contact pressure and sliding velocity as a result of the multicontact nature of the sliding interface. Associated changes in the local density of microcontacts are evidenced from variations in the distribution of the light intensity transmitted through the rough contact interface. From separate static indentation experiments, it is shown that all the light intensity data obtained locally at various contact loads and contact locations can be represented in the form of a single master curve, which strongly supports the scaling of the transmitted light with the nominal contact pressure, at least for the considered rough surface. Accordingly, the theoretical prediction of a linear relationship between the proportion of area in contact and contact pressure is retrieved experimentally. More importantly, the combination of local stress and light intensity measurements allowed us to separate the contributions of two mechanisms when contact pressure or velocity is varied. The first one consists in a decrease in the local density of microcontacts when the pressure decreases or the sliding velocity increases. The second one encompasses all the frictional dissipative processes occurring within microasperity contacts. A comparison between smooth and rough contacts suggests that dissipative processes occurring at the interface predominate over viscoelastic dissipation at microasperity scale. More generally, these results open the way to a close reexamination of the validity of the hypothesis embedded in most rubber friction models, especially the assumption that friction can be separated into an adhesive and an hysteretic component.

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APPENDIX A: LINEAR VISCOELASTIC MEASUREMENTS

The selected epoxy rubber is characterized by a crystallization of the flexible chains of the polyether-diamine crosslinker at low temperature (−20 °C). As a result, it is not possible to determine the room temperature viscoelastic modulus of the rubber over an extended frequency range using the usual route of master curves and time-temperature superposition principle. Instead, we used two complementary techniques to determine the frequency dependence of the viscoelastic modulus at room temperature. Up to 20 Hz, the shear modulus was measured using conventional dynamical mechanical thermal analysis (DMTA). Elastomer disks 2 mm in thickness and 8 mm in diameter are sheared at low strain (0.05 %) between the parallel plates of a rheometer (Anton Paar, MCR 501). The shear modulus is measured at room temperature during a frequency sweep between 50 and 0.01 Hz. In the high-frequency range (up to 10 kHz), the viscoelastic modulus is measured using surface fluctuation specular reflection (SFSR) spectroscopy, a technique based on the principle that surface fluctuations reveal the properties of the medium. The principle of this technique is fully described in Refs. [27,28]. The results of both viscoelastic measurements are shown in Fig. 13.

APPENDIX B: INVERSION OF THE DISPLACEMENT FIELD: COMPARISON BETWEEN GREEN’S TENSOR AND FINITE ELEMENT CALCULATIONS

In order to evaluate the influence of finite strains on the inversion of displacement fields, the same azimuthal displacement profile was inverted using both a linear elastic approach based on Green’s tensor [16] and a finite element (FE) inversion procedure which is fully described in Ref. [14]. As opposed to Green’s tensor calculations, the FE inversion is able to take into account both the geometrical and material nonlinearities (neo-Hookean behavior of the rubber) of the problem. As shown in Fig. 14, identical shear stress profiles are provided by both methods. In other words, the occurrence of finite strains at the edge of the contact (see Fig. 5) does not induce any significant error in the stress field deduced from an inversion using a linear elastic analysis. It should be noted that this conclusion is opposed to that drawn for linear sliding conditions: In this case, finite strains were found to alter significantly the accuracy of linear inversions [14]. Some theoretical justifications for this difference can be found in finite strain analytical calculations [15].


[15] Some theoretical justifications for this difference can be found in finite strain analytical calculations, which show that a linear contact mechanics description of torsional contacts remains valid up to the third order in the applied twist angle, C. Y. Herbert (private communication).


